TABLE I. Combinations of elastic constants governing pure mode propagation in cubic crystals.

-	Propagation direction	Particle motion	Туре	Elastic constants
	Γ100]	[100]	Longitudinal	C_{11}
	[110]	[110]	Shear	$(C_{11}-C_{12})/2$
	[100]	⊥ to [100]	Shear	C ₄₄
	[110]	[110]	Longitudinal	$(C_{11}+C_{12}+2C_{44})/2$
	[110]	[001]	Shear	C44
	[111]	[111]	Longitudinal	$(C_{11}+2C_{12}+4C_{44})/3$
	Γ1117	⊥ to [111]	Shear	$(C_{11}-C_{12}+C_{44})/3$

and Ruoff⁸ assumed a linear variation of Δ vs P as described below. We note that

$$\rho = \rho_0 \lambda^3. \tag{14}$$

Beginning with Eq. (9) and substituting for B^S and ρ from (12) and (14), we obtain

$$\Delta(P) = \frac{T\beta^2 \{ [L_1^2(P=0)/\tau_1^2(P)] - \frac{4}{3} [L_2^2(P=0)/\tau_2^2(P)] \}}{\lambda^2 C_P} .$$

Next express $\Delta(P)$ as a power-series expression.

$$\Delta(P) = \Delta_0 + \Delta_0' P + \Delta_0''(P^2/2) + \cdots.$$
 (16)

The logarithmic derivative of Δ as given by (15) yields

$$\Delta^{-1} \left(\frac{\partial \Delta}{\partial P} \right)_{T} = \frac{2}{\beta} \left(\frac{\partial \beta}{\partial P} \right)_{T} - \frac{2}{\lambda} \left(\frac{\partial \lambda}{\partial P} \right)_{T}$$

$$- \left(\frac{L_{1}^{2} (P=0)}{\tau_{1}^{2} (P)} - \frac{4}{3} \frac{L_{2}^{2} (P=0)}{\tau_{2}^{2} (P)} \right)^{-1} \frac{\partial}{\partial P}$$

$$\times \left(\frac{L_{1}^{2} (P=0)}{\tau_{1}^{2} (P)} - \frac{4}{3} \frac{L_{2}^{2} (P=0)}{\tau_{2}^{2} (P)} \right)_{T} - C_{P}^{-1} \left(\frac{\partial C_{P}}{\partial P} \right)_{T}. \tag{17}$$

We now proceed to evaluate $(\partial \Delta/\partial P)_T$ as $P\rightarrow 0$, i.e., Δ_0' . From Eq. (6) we have

$$\lim_{P \to 0} -(2/\lambda) \left(\frac{\partial \lambda}{\partial P} \right)_T = -2/3 B_0^T. \tag{18}$$

Table II. Internal consistency of the adiabatic elastic constant values (in units of 10¹¹ dyn/cm²) of RbCl, RbBr, and RbI as a function of temperature (°K) at 1 atm.

(15)

		C_{11}		C_{12}		C ₄₄	
	Temperature	(1)a	(2)b	(1)a	(2)b	(1) a	(2) b
III RbI							
	300	2.5570	2.5561	0.3766	0.3815	0.2772	0.2777
	260	2.6496	2.6519	0.3675	0.3641	0.2792	0.2799
	220	2.7490	2.7474	0.3514	0.3506	0.2818	0.2810
	180	2.8504	2.8502	0.3354	0.3352	0.2840	0.2844
I RbCl							
	300	3.6213	3.6242	0.6154	0.6124	0.4668	0.4678
	260	3.7486	3.7519	0.6070	0.6034	0.4713	0.4714
	220	3.8756	3.8831	0.5934	0.5899	0.4754	0.4754
	180	4.0011	4.0071	0.5753	0.5745	0.4789	0.4794
II RbBr							
	300	3.1513	3.1522	0.4995	0.5000	0.3798	0.3801
	260	3.2570	3.2624	0.4825	0.4860	0.3831	0.3834
	220	3.3691	3.3727	0.4714	0.4731	0.3863	0.3866
	180	3.4882	3.4882	0.4587	0.4593	0.3898	0.3900

^a From the experimental runs at higher pressures as a function of temperature.

 $^{^{\}rm b}$ From the experimental runs at one atmosphere as a function of temperature.

Table III. Adiabatic elastic constants (in units of 10¹¹ dyn/cm²) and density (in units of g/cm³) of RbCl as a function of temperature (°K) as obtained in present work (PW) and those obtained by Marshall, Pederson, and Dorris (MPD).

Temp.	Cn		C_{12}		C ₄₄		Bulk modulus		Density		
	PW	MPD	PW	MPD	PW	MPD	PW	MPD	PW	MPD	Δ
300	3.6242	3.653	0.6124	0.645	0.4678	0.478	1.616	1.647	2.7969	2.7972	0.0533
280	3.6894		0.6053		0.4695		1.633		2.8033		0.0502
260	3.7519		0.6034		0.4714		1.653		2.8097		0.0471
240	3.8189	3.840	0.5959	0.666	0.4735	0.482	1.670	1.724	2.8160	2.8163	0.043
220	3.8831		0.5899		0.4754		1.688		2.8223		0.040
200	3.9448		0.5812		0.4775		1.702		2.8285		0.036
180	4.0071	4.025	0.5745	0.676	0.4794	0.486	1.719	1.792	2.8346	2.8345	0.033
160	4.0681		0.5630		0.4813		1.731		2.8404		0.0293
140	4.1194		0.5569		0.4831		1.744		2.8458		0.025
120	4.1792	4.206	0.5516	0.676	0.4848	0.490	1.761	1.852	2.8504	2.8507	0.0214
100	4.2394	4.266	0.5484	0.676	0.4858	0.491	1.779	1.873	2.8538		0.0172

We also have the following thermodynamic relation:

$$(\partial \beta/\partial P)_T = -\left[(\partial/\partial T) (1/B^T) \right]_P. \tag{19}$$

This is true at all pressures, but in the limit we have

$$\lim_{P \to 0} (\partial \beta / \partial P)_T = (1/B_0^{T^2}) (\partial B^T / \partial T)_{P=0}.$$
 (20)

Likewise

$$(\partial C_P/\partial P)_T = -T[(\partial^2/\partial T^2)(1/\rho)]_P$$

= $-(T/\rho)[(\partial\beta/\partial T)_P + \beta^2].$ (21)

Again at the limit we have

$$\lim_{P\to 0} (\partial C_P/\partial P)_T = - (T/\rho_0) [(\partial \beta/\partial T)_{P=0} + \beta_0^2]. \quad (22)$$

Therefore all the terms on the right-hand side of Eq. (17) are known in the limit as $P\rightarrow 0$ if we have sufficient thermal expansion and specific-heat data as a function of temperature at zero pressure to combine with the direct experimental values which we measure and which give the second and third terms. Thus we can evaluate Δ_0 '. Hence we have

$$\Delta(P) = \Delta_0 + \Delta_0' P$$

Table IV. Temperature derivatives of the adiabatic elastic constants (in units of 10⁷ dyn/cm² °K) of RbCl at room temperature.

	Temper-				Bulk
	(°K)	C ₁₁	C_{12}	C ₄₄	modulus
Present	300	-30.80	3.40	-0.934	-8.00
Haussuhl	295	-32.12	3.46	-1.094	-8.40
Marshall et al.	300	-31.10	-3.50	-0.667	-12.7

which is then substituted into Eq. (13). Thus we can evaluate λ from (13) and then we get all the pertinent elastic constants. (Note that one does not have to have approximate values of $(\partial B_0^S/\partial P)_T$ to carry out this analysis.) Combinations of elastic constants for puremode propagation in cubic crystals are given in Table I. In the following sections the elastic constants of RbCl, RbBr, and RbI as a function first of temperature at one atmosphere and then of pressure at several temperatures are discussed. The values presented are (i) based on the travel times evaluated at the resonant frequency of quartz at a pressure P and temperature T. (ii) They are the least-square estimates obtained from four $\rho(P)v(P)$ values, and (iii) they are internally self-consistent. As an example of self-consistency we present the values of the elastic constants of RbCl, RbBr, and RbI as a function of temperature at one atmosphere in Table II. The two values of each constant at a temperature are obtained from two independent experimental runs as indicated underneath Table II. The agreement between these pairs of values are within the range of experimental errors. These errors are estimated to be 0.2%, 0.6%, and 0.4% for C_{11} , C_{12} , and C_{44} , respectively, for each of the rubidium halides. The errors associated with these values of the elastic constants incorporate not only the usual errors of measurements like length of the specimens, absolute null frequency and its reproducibility, and misorientation, but also the statistical or random errors due to replication. The associated errors are thus larger in magnitude than the precision with which each experimental run could be executed. Where some pertinent ancillary data were not available, specific assumptions had to be made. These assumptions are explicitly described in the separate sections dealing with the halides to which they specifically